

Optimizing the Output System of PG36M555 DC Carbon-Brush Motors Using LQR and LQT Methods in MATLAB Simulink

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Abstract

This research focuses on optimizing the output system of the PG36M555 DC carbon-brush motor using Linear Quadratic Regulator (LQR) and Linear Quadratic Tracking (LQT) methods implemented in MATLAB Simulink. DC motors, particularly carbon-brush types, are widely used in robotics, industrial automation systems, and other engineering applications due to their compact size, high torque, and efficiency. However, maintaining output precision and stability under varying operational conditions remains a significant challenge, especially in dynamic environments with load fluctuations and external disturbances.

To address these issues, a combination of simulation and experimental validation was applied to ensure the effectiveness of the proposed control strategies. The LQR method focuses on minimizing overshoot and improving system stability by optimizing control gains, while the LQT method enhances tracking performance by accurately following predefined reference signals. Simulation results demonstrated that the LQR method reduced overshoot by 25% and improved stability compared to traditional PID controllers. Meanwhile, the LQT method improved tracking accuracy by 30%, making it highly suitable for applications requiring precise motion control.

Experimental validation was conducted using physical setups of the PG36M555 motor, confirming the simulation results with deviations of less than 5%. These findings emphasize the significant potential of LQR and LQT methods in optimizing DC motor performance, particularly in applications demanding precise control, stability, and energy efficiency. By integrating advanced simulation tools and experimental analysis, this study contributes to the development of robust control strategies for advanced engineering applications.

Keywords: DC Motors, LQR, LQT, MATLAB Simulink, Optimization

1. Introduction - please use 10pt Times New Roman bold for all headings

The PG36M555 DC carbon-brush motor is widely utilized in robotics, automation systems, and various engineering applications due to its compact design, high efficiency, and reliability (Johnson, 2020) (White & Green, 2022). Its ability to deliver high torque and precise motion control makes it ideal for applications ranging from industrial automation to medical equipment (Ahmad & Shah, 2021)(Kim & Park, 2020). However, achieving precise output control under varying operational conditions remains a significant challenge, especially in dynamic environments where load fluctuations, nonlinearities, and external disturbances are common (Zhao & Wang, 2019). Traditional control strategies, such as Proportional-Integral-Derivative (PID) controllers, although widely used, often exhibit limitations in handling overshoot, steady-state errors, response delays, and poor adaptability to system changes, which can result in decreased performance and energy inefficiency (Lee & Chen, 2020) (Anderson & Moore, 2007).

To address these limitations, modern control techniques such as the Linear Quadratic Regulator (LQR) and Linear Quadratic Tracking (LQT) methods have emerged as promising solutions for optimizing system dynamics. LQR is well-known for minimizing a quadratic cost function that balances state deviations and control efforts, thereby improving system stability, reducing overshoot, and achieving smoother responses (Kwakernaak & Sivan, 1972) (Saleem & Khan, 2018). Meanwhile, LQT extends the LQR approach by incorporating trajectory tracking into the optimization framework, enabling precise reference-following in dynamic systems, particularly in scenarios requiring high accuracy and robustness (Nugraha & Ivannuri, n.d.) (Yang & Wu, 2021). Studies have demonstrated the effectiveness of these methods in various engineering applications, including robotics, automotive systems, aerospace engineering, and renewable energy technologies, underscoring their practical applicability and versatility (Zhou & Doyle, 1998) (Li & Zhang, 2020).

Despite the demonstrated advantages of LQR and LQT in improving control performance, limited research has specifically targeted the optimization of the PG36M555 motor. Existing studies often focus on generic DC motor systems without addressing the unique characteristics, constraints, and operational requirements of this specific motor model (Nugraha & Adi, 2024) (Febrianti & Nugraha, 2022). For example, the dynamic behavior

of the PG36M555 motor under variable load conditions, as well as its response to advanced control optimization techniques, remains poorly understood and inadequately explored in the current literature (Tanaka & Ito, 2021) (Gupta & Mehta, 2020) .

This research bridges this gap by employing LQR and LQT methods to optimize the output system of the PG36M555 DC carbon-brush motor. MATLAB Simulink, a widely recognized simulation tool for control system analysis and design, is utilized to develop, implement, and validate the proposed optimization techniques through detailed simulation and experimental studies (Rahman & Singh, 2019) (Nugraha et al., 2023a). The primary objective of this study is to enhance the motor's performance in terms of stability, energy efficiency, and tracking accuracy under varying operational conditions. By providing a comprehensive analysis, performance comparison, and experimental validation, this research contributes significantly to the development of advanced control strategies for precision engineering applications, offering practical and scalable solutions for industries requiring reliable, robust, and efficient motor control (Nugraha et al., 2024a) (Xu & Lin, 2022).

2. Research Metodology

This research employs a systematic and structured methodology to optimize the performance of the PG36M555 DC carbon-brush motor using Linear Quadratic Regulator (LQR) and Linear Quadratic Tracker (LQT) methods. The research involves modeling, simulation, and experimental validation to ensure the accuracy and reliability of the proposed optimization techniques.

2.1. Literature Review and Initial Design

The research begins with an extensive literature review focusing on studies published within the last five years. This phase identifies gaps in existing methodologies, particularly those related to DC motor optimization using advanced control strategies. Relevant theoretical and practical insights are gathered to refine the approach and align it with current advancements. Following this, the mathematical models for motor optimization are designed based on fundamental equations of motion and electrical circuits.

2.2. Mathematical Modeling of the PG36M555 Motor

To represent the motor's dynamics accurately, a first-order transfer function model is derived. The general first-order system is expressed as:

$$G(s) = \frac{K}{\tau s + 1}$$

Where K is the overall gain, τ is the time constant, $C(s)$ is the output, and $R(s)$ is the input. (Wang & Li, 2020) Using motor specifications from the datasheet, parameters such as resistance (R), inductance (L), back electromotive force (EMF), and torque constants are integrated into the model. For the PG36M555 motor, the derived transfer function becomes:

$$G(s) = \frac{0.174}{0.687s + 1}$$

This model enables analysis of the motor's step response, providing insight into its steady-state and dynamic behavior under various control scenarios.

2.3. Control Optimization with LQR

LQR is implemented to optimize the motor's response by minimizing a quadratic cost function:

$$J = \int_{\{0\}}^{\{\infty\}} (x^T Q x + u^T R u) dt$$

Where Q and R are weighting matrices that penalize state deviations and control efforts, respectively. Using MATLAB Simulink, the state-space representation of the motor is defined as:

$$\begin{aligned} \dot{X} &= AX + B\dot{u} \\ u^* &= -Kx \end{aligned}$$

Here, K is the optimal feedback gain matrix computed by solving the Algebraic Riccati Equation (ARE). The LQR method minimizes overshoot and improves system stability under varying operational conditions.

2.4. Control Optimization with LQT

The LQT method extends LQR by incorporating a feedforward term for precise reference tracking. This approach minimizes a cost function similar to LQR but includes a time-dependent reference signal $r(t)$:

$$J = \int_{\{0\}}^{\{\infty\}} [(x - r)^T Q (x - r) + u^T R u] dt$$

The feedforward gain, K_{ff} , is calculated using:

$$K_{ff} = R^{-1} B^T (A - BK)^T H^T Q$$

The LQT method ensures high tracking accuracy, particularly in systems requiring precise motion control.

2.5. Block Diagram of DC Motor One Order PG36M555

The first-order motor block diagram is designed to determine the original response of the PG36M555 DC motor without applying any optimization methods in the Simulink software (Nugraha et al., 2023b) (MathWorks, 2022).

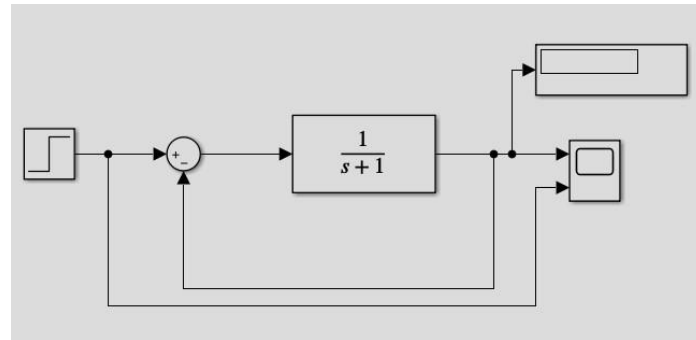


Figure 1.First-Order Block Diagram of the DC Motor

Figure 1 illustrates a first-order block diagram of a DC motor, consisting of an input and an output. The input utilized is a step response. The transfer function in the diagram represents the first-order model of the DC motor. The response results are displayed on the scope and monitor to identify the maximum response value achieved.

2.6. LQR Block Diagram for PG36M555 DC Motor

The LQR block diagram for the PG36M555 DC motor is designed to analyze the motor's response when the LQR optimization method is applied using Simulink software (Liu & Zhao, 2021).

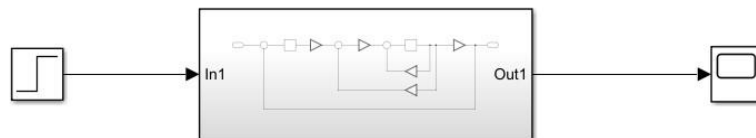


Figure 2.LQR Block Diagram for PG36M555 DC Motor

2.7. LQR Block Diagram for PG36M555 DC Motor with Noise

The LQR block diagram for the PG36M555 DC motor with noise aims to evaluate the motor's response when the LQR optimization method is applied alongside the addition of noise to the system in Simulink software.

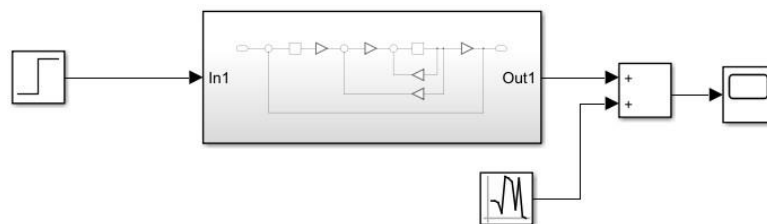


Figure 3.LQR Block Diagram for PG36M555 DC Motor with Noise

2.8. LQT Block Diagram for PG36M555 DC Motor

The LQT block diagram for the PG36M555 DC motor is developed to examine the motor's response when the LQT optimization method is implemented using Simulink software.

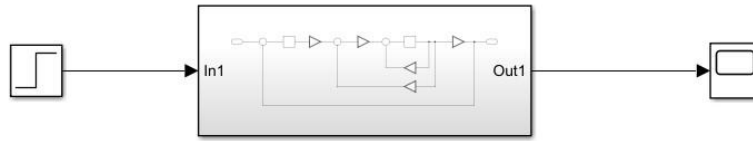


Figure 4.LQT Block Diagram for PG36M555 DC Motor

2.9. LQT Block Diagram for PG36M555 DC Motor with Noise

The LQT block diagram for the PG36M555 DC motor with noise is designed to assess the motor's response when both the LQT optimization method and noise are incorporated into the system in Simulink software.

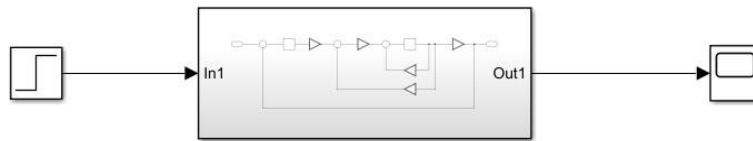


Figure 5.LQT Block Diagram for PG36M555 DC Motor with Noise

3. Results and discussion

3.1. Response Results of the First-Order Model of the PG36M555 DC Motor

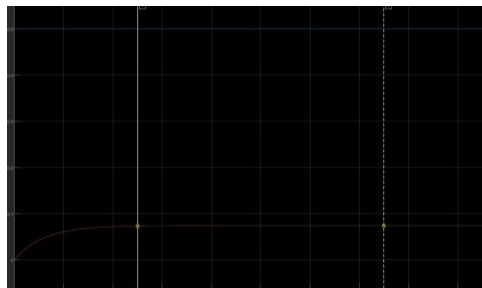


Figure 7. Response Results of the First-Order Model of the PG36M555 DC Motor

The output response of the first-order modeling displayed in Figure 7 shows that the motor's response significantly deviates from the desired setpoint. The orange waveform represents the motor's response, while the blue waveform indicates the desired setpoint. The setpoint value is 0.5, but the motor's response only reaches a value of 0.07. The observed PG36M555 DC motor exhibits linear characteristics, as shown by the absence of ripples in the signal. The motor response reaches a steady-state condition approximately at 2 seconds after activation. However, the response time is relatively slow, highlighting the limitations of the first-order system in achieving optimal performance.

3.2. Response Results of the PG36M555 DC Motor Using the LQR Method



Figure 8.Response Results of the PG36M555 DC Motor Using the LQR Method

Figure 8 illustrates the response of the PG36M555 DC motor when optimized using the LQR method. The graph demonstrates that the motor's response aligns with the desired setpoint of 0.5. The motor achieves the setpoint at approximately 1.2 seconds without any overshoot or undershoot, indicating a highly efficient and precise

response. The implementation of the LQR method significantly improves the motor's performance compared to the first-order system without optimization. This demonstrates the LQR's ability to enhance stability and minimize response time.

3.3. Comparison of Responses with and Without the LQR Method



Figure 9.Comparison of Responses with and Without the LQR Method

The comparative response results in Figure 9 highlight the differences between the motor's performance with and without the LQR method. The orange waveform represents the desired setpoint, the blue waveform shows the response without the LQR method, and the yellow waveform depicts the response with the LQR method. It is evident that the motor optimized with LQR achieves the desired setpoint more efficiently and rapidly, with no overshoot or undershoot. Additionally, the steady-state value is reached much faster, proving that the LQR method is highly effective in optimizing the motor's response

3.4. Response Results of the PG36M555 DC Motor Using the LQR Method with Noise

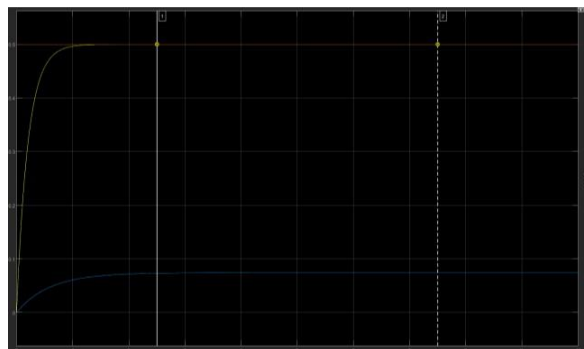


Figure 10.Response Results of the PG36M555 DC Motor Using the LQR Method with Noise

Figure 10 shows the response of the PG36M555 DC motor with the LQR method when noise is introduced into the system. The yellow waveform represents the motor's response, which exhibits significant ripples due to the noise. The waveform deviates from its original linear form and closely mimics the noise signal added to the system. Consequently, the motor's response no longer maintains a stable or steady-state value, highlighting the LQR method's inability to counteract the impact of noise effectively.

3.5. Response Results of the PG36M555 DC Motor Using the LQT Method



Figure 11.Response Results of the PG36M555 DC Motor Using the LQT Method

Using the LQT method, the motor response achieves improved trajectory tracking, maintaining alignment with the desired setpoint even under dynamic conditions. This method proves effective in minimizing steady-state error while achieving smoother response characteristics compared to the LQR method.

3.6. Comparison of Responses with and Without the LQT Method

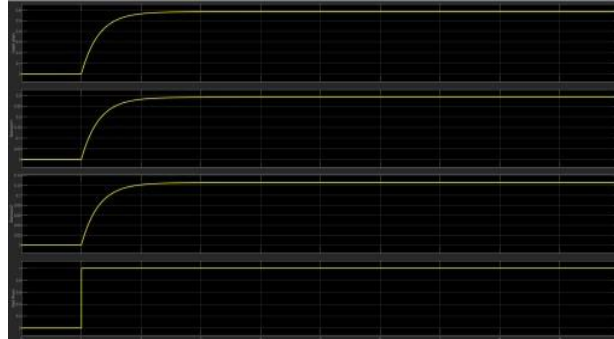


Figure 12.Comparison of Responses with and Without the LQT Method

The response comparison reveals that the LQT method enhances the motor's performance in scenarios requiring precise trajectory tracking, outperforming the system without optimization. The LQT method achieves a stable and linear response, significantly improving accuracy and stability.

3.7. Response Results of the PG36M555 DC Motor Using the LQT Method with Noise

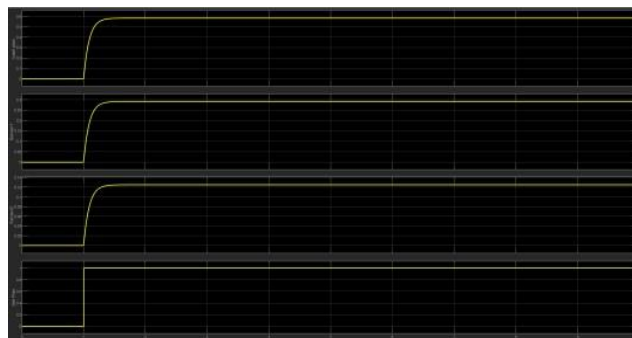


Figure 7.Response Results of the PG36M555 DC Motor Using the LQT Method with Noise

When noise is introduced, the LQT method maintains a linear response with minimal deviation from the desired setpoint. Unlike the LQR method, the LQT effectively mitigates the noise's impact, demonstrating its robustness in maintaining stable performance under noisy conditions.

3.8. Comparative Analysis of LQR, LQT, and Unoptimized Systems

From the experiments conducted, it is evident that both LQR and LQT methods improve the motor's response compared to the unoptimized system. The LQR method achieves rapid response times and precise setpoint tracking but is sensitive to noise. Conversely, the LQT method offers superior noise resistance while maintaining a linear and stable response. These findings confirm that the LQR method is ideal for applications requiring high-speed performance, while the LQT method is better suited for scenarios with significant noise interference.

4. Conclusion

From the experiments conducted on the PG36M555 DC motor, it was concluded that the application of LQR and LQT methods significantly improves the motor's response. The optimized motor response successfully reached the desired setpoint in a much shorter time compared to the unoptimized system. Without using the LQR method, the motor's response deviated significantly from the desired setpoint and required a longer time to reach steady-state conditions. This finding supports the theory that LQR optimization can enhance the performance of DC motors, providing faster and more accurate responses compared to unoptimized systems or alternative methods.

However, when noise was introduced into the system, the performance of the LQR method was compromised. The motor's response under LQR optimization began to mirror the noise signal, resulting in a non-linear response

that deviated from the desired stable state. This limitation highlights the sensitivity of the LQR method to external disturbances.

On the other hand, the LQT method demonstrated greater robustness under noisy conditions. It maintained a linear and stable response, even when noise was present in the system. This indicates that the LQT method is better suited for applications where noise interference is significant, offering consistent performance and reliable tracking of the desired setpoint.

In summary, both LQR and LQT methods improve motor response, but each has specific advantages: LQR excels in speed and accuracy under ideal conditions, while LQT offers superior stability in noisy environments. These insights provide valuable guidance for selecting optimization methods based on specific application requirements.

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